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Equation of State of Sodium Chloride

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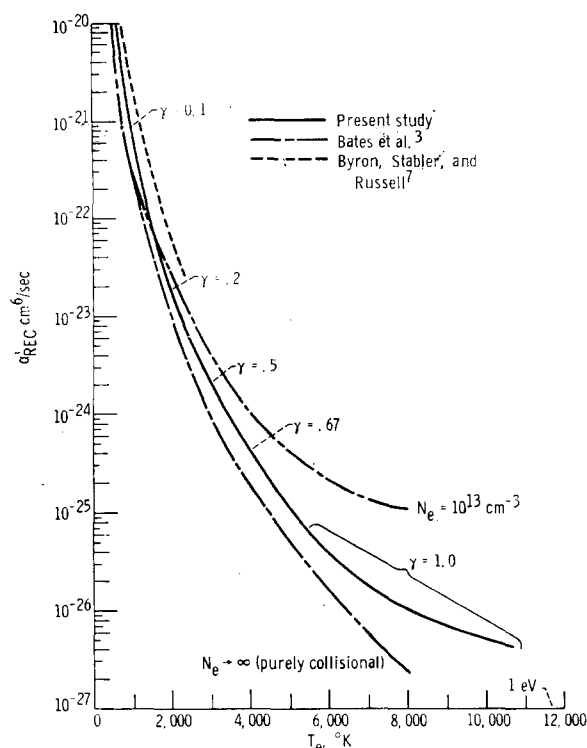


FIG. 3. Argon and hydrogen three-body collisional recombination coefficients as functions of electron temperature for range of electron number density (10^{13} – 10^{18} cm^{-3}).

The three-body coefficient α_{rec} from several sources is plotted versus T_e in Fig. 1. For the curve from Ref. 8, the quantum gaps which correspond to the minimum de-excitation rates are indicated. The dashed curve gives the results of Ref. 7 for potassium, while the broken curves from Ref. 3 are for a pseudoalkali atom plasma. The coefficient from Ref. 3 is a function of number density N_e because radiative de-excitation and two-body capture are included. The experimental results of Cool and Zukoski⁹ for potassium-seeded argon with T_e from 1800° to 3200°K agree closely with the results of Ref. 8. Experimental points are shown for both pure cesium and cesium-seeded argon.^{10–12} The agreement between theory and experiment for the alkalis is well within the expected accuracy of the Gryzinski cross sections.^{3,8}

The disparity between the theoretical¹³ (Gryzinski, total excitation) and experimental¹⁴ (first excitation, $\approx 90\%$ total excitation) monoenergetic cross sections (in cm^2) and Maxwell averaged total excitation coefficients (in cm^3/sec) can be seen for potassium and cesium from Fig. 2. The agreement will be less satisfactory for nonhydrogenic atoms and there may be some ambiguity as to choice of upper states for excitation calculations. Using more accurate excitation cross sections may not always improve the recombination calculation because radiative emission may be important in both recombination experiments and MHD systems. The contribution of this deexcitation mechanism depends on the superelastic collision rate and optical absorption cross section of the ionized species.^{2,7,8}

Values of α_{rec} for argon were calculated in the same fashion as the cesium coefficients. At the lower electron temperatures, 500° to 3000°K, the γ factor was fixed by fitting the results between the curves from Refs. 3 and 4. This procedure is necessary because of the approximation of “collapsed” quantum states.⁸

The α_{rec} for argon is plotted vs T_e in Fig. 3 and compared with the hydrogen results of Refs. 3 and 7. Some discrepancy between the results of Ref. 3 and the present study is due to the

difference between the Maxwell averaged first excitation cross sections of argon and hydrogen. The neglect of radiative deexcitation in the present calculation is of less importance, as was pointed out in Ref. 8 where the mean radiative transition probabilities were compared with the superelastic collision frequencies.⁸ It has been shown that the purely collisional approach is a good approximation for cesium,⁸ while the maximum radiative correction for argon is 50% at $T_e = 10\,000^\circ\text{K}$.

For nonequilibrium MHD power generation, recombination rates will not be very different for carrier and seed gases at achievable electron temperatures.¹ However, the average energy lost by the free electrons in recombination will depend on the mechanism by which the captured electrons become deexcited. Results of Ref. 2 indicate that emission of radiation is not an important energy loss process for potassium in argon. Collisional deexcitation frequencies from Ref. 8 indicate that this is also true for cesium in argon. However, a more complete study of the plasma energy balance incorporating accurate cross sections for ionization, excitation, and resonance absorption is desirable.

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Equation of State of Sodium Chloride

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BECAUSE of many requests, I wish to publish the following numerical table of results for the equation of state of NaCl as calculated in an earlier paper¹ along with a few comments on various proposed equations for NaCl. Table I gives the pressure in kilobars at the corresponding values of $\Delta a/a_0$ and temperature in the appropriate row and column. The parameter $\Delta a/a_0$ is the fractional compression of the lattice parameter where the standard value a_0 is the appropriate lattice parameter at zero pressure and 25°C. The increments between the values given in the table were chosen such that one can linearly interpolate between the tabulated values to an accuracy of better than 0.02 kbar.

In recent years several equations have been proposed to give the volume change vs pressure for NaCl at room temperature.^{2,3} A comparison of these equations and the results in Table I is given in Fig. 1 along with experimental measurements by Bridgman,⁴ Christian,⁵ and Perez-Albuern and Drickamer.³ This figure gives the differences in $\Delta V/V_0$ of the respective equations or experimental measurements at a specified pressure to the $\Delta V/V_0$ calculated in Ref. 1. at that pressure. Experimental values of NaCl compression have been measured by Jeffery *et al.*⁶ at the pressure of the bismuth I–II phase transition. If the value of 25.4 kbar⁷ is accepted for the Bi I–II transition, then Jeffery's measurement of $\Delta V/V_0 = -0.084 \pm 0.02$ for the compression of NaCl at this transition gives one point at which both P and V are simultaneously known. This point is shown by the large square in Fig. 1. It is noted that all results agree to within the accuracy of the x-ray measurement at 25.4 kbar except Murnaghan's equation em-

TABLE I. Calculated pressure at given compressions and temperatures from 0-500 kbar and 0°C-mp for NaCl. Based on equation of state by Decker.*

$\frac{\Delta s}{s_0}$	0 c	25 c	100 c	200 c	300 c	400 c	500 c	600 c	700 c	800 c	900 c	1000 c	1200 c	1400 c	1600 c	1800 c	2000 c
0.040										0.45							
0.038										1.25	4.03						
0.036										2.09	4.87						
0.034										2.94	5.74						
0.032										1.03	3.83	6.63					
0.030										1.94	4.75	7.55	10.36				
0.028										2.88	5.69	8.51	11.32				
0.026										1.03	3.85	6.67	9.49	12.31			
0.024										2.02	4.83	7.67	10.50	13.33			
0.022										3.04	5.87	8.71	11.55	14.39			
0.020										1.25	4.10	6.93	9.78	12.62	15.47		
0.018										2.33	5.18	8.03	10.88	13.74	16.59		
0.016						0.60				3.45	6.30	9.16	12.02	14.88	17.74	23.47	
0.014						1.74				4.56	7.46	10.32	13.19	16.06	18.93	24.67	
0.012						2.92				5.78	8.65	11.52	14.40	17.28	20.15	25.91	
0.010						4.13				7.00	9.88	12.76	15.64	18.53	21.41	27.19	
0.008						2.50				5.38	8.26	11.15	14.03	16.93	19.82	22.71	28.50
0.006				0.92		3.79				9.56	12.45	15.35	18.25	21.15	24.05	29.86	
0.004				2.24		5.11				8.00	10.90	13.80	16.70	19.61	22.52	25.43	31.25
0.002				3.59		6.47				9.37	12.27	15.18	18.09	21.01	23.92	26.84	32.68
0.000			0.73	4.99		7.88				10.78	13.69	16.61	19.53	22.45	25.38	28.33	34.16
-0.002	0.74	0.00	2.12	4.99		7.88				12.27	15.18	18.09	21.01	23.92	26.84	29.80	40.02
-0.004	2.21	0.00	3.56	6.43		9.33				15.16	18.08	21.01	23.94	26.87	29.80	32.74	41.56
-0.006	4.42	2.21	5.03	7.91		10.82				16.66	19.59	22.53	25.47	28.41	31.34	34.28	43.13
-0.008	6.89	3.72	4.42	6.56		9.44				15.28	18.21	21.15	24.10	27.04	29.99	32.94	44.75
-0.010	5.28	5.99	8.12	11.02		13.93				16.87	19.81	22.76	25.71	28.66	31.62	34.58	46.32
-0.012	6.89	7.60	9.74	12.64		15.56				18.50	21.45	24.41	27.37	30.33	33.30	36.26	47.90
-0.014	8.55	9.26	11.40	14.38		17.24				20.19	23.15	26.11	29.07	32.05	35.02	37.99	49.50
-0.016	10.26	10.97	13.12	16.03		18.97				21.92	24.89	27.86	30.84	33.81	36.80	39.78	51.12
-0.018	12.02	12.73	14.88	17.80		20.75				23.71	26.68	29.66	32.65	35.63	38.62	41.62	52.79
-0.020	13.83	14.54	16.70	19.62		22.58				25.55	28.53	31.51	34.51	37.50	40.50	43.50	54.50
-0.022	15.69	16.40	18.56	21.50		24.46				27.44	30.43	33.40	36.42	39.43	42.39	45.45	56.51
-0.024	17.61	18.32	20.49	23.43		26.40				29.39	32.38	35.38	38.39	41.40	44.43	47.44	58.54
-0.026	19.59	20.30	22.47	25.42		28.40				31.39	34.39	37.40	40.42	43.44	46.46	49.49	60.59
-0.028	21.62	22.33	24.51	27.46		30.45				33.45	36.46	39.48	42.50	45.53	48.57	51.60	62.74
-0.030	23.71	24.43	26.61	29.57		32.56				35.57	38.59	41.62	44.65	47.68	50.71	53.77	64.91
-0.032	25.87	26.58	28.77	31.73		34.73				37.75	40.78	43.81	46.85	49.90	52.95	56.00	67.11
-0.034	28.08	28.80	30.00	33.66		36.97				39.99	43.03	46.07	49.12	52.17	55.24	58.29	69.31
-0.036	30.36	31.08	33.27	36.25		39.26				42.30	45.34	48.39	51.45	54.51	57.48	60.66	71.57
-0.038	32.71	33.43	35.62	38.61		41.63				44.67	47.72	50.78	53.85	56.91	60.00	63.08	73.82
-0.040	35.12	35.84	38.04	41.03		44.06				47.11	50.17	53.23	56.31	59.39	62.48	65.56	76.15
-0.042	37.60	38.32	40.53	43.52		46.56				49.61	52.68	55.76	58.84	61.93	64.99	68.11	78.56
-0.044	40.15	40.87	43.08	46.09		49.13				52.19	55.27	58.35	61.44	64.54	67.65	70.74	81.03
-0.046	42.78	43.50	45.71	48.72		51.77				54.84	57.93	61.02	64.12	67.22	70.33	72.67	83.15
-0.048	45.47	46.20	48.41	51.43		54.49				57.57	60.66	63.76	66.86	69.96	73.10	76.21	85.32
-0.050	48.25	48.97	51.19	54.22		57.28				60.37	63.47	66.57	69.69	72.81	75.94	79.08	88.59
-0.052	51.10	51.82	54.05	57.08		60.15				63.20	66.35	69.47	72.59	75.72	78.86	82.00	91.29
-0.054	54.03	54.78	56.98	60.02		63.10				66.20	69.36	72.44	75.57	78.71	81.86	85.00	94.35
-0.056	57.04	57.80	60.00	63.05		66.13				69.24	72.36	75.50	78.64	81.78	84.94	88.09	97.59
-0.058	60.14	60.87	63.10	66.15		69.25				72.36	75.50	78.64	81.78	84.94	88.09	91.27	100.70
-0.060	63.32	64.05	66.29	69.35		72.45				75.57	78.71	81.86	85.00	88.15	91.30	94.54	103.91
-0.062	66.59	67.32	69.57	72.63		75.74				78.87	82.02	85.17	88.34	91.51	94.70	97.88	107.27
-0.064	69.95	70.68	72.93	76.00		79.12				82.26	85.41	88.58	91.75	94.91	98.13	101.31	110.69
-0.066	73.41	74.14	76.39	79.47		82.59				85.74	88.90	92.08	95.26	98.44	101.66	104.84	114.24
-0.068	76.96	77.69	79.94	83.03		86.15				89.31	92.48	95.67	98.86	102.05	105.27	108.47	118.00
-0.070	80.60	81.34	83.59	86.68		89.82				92.98	96.16	99.35	102.55	105.76	108.98	112.19	121.99
-0.072	84.35	85.08	87.34	90.44		93.58				96.75	99.94	103.14	106.35	109.56	112.79	116.07	125.97
-0.074	88.20	88.93	91.20	94.30		97.45				100.63	103.82	107.03	110.25	113.47	116.71	119.93	129.93
-0.076	92.15	92.88	95.15	98.26		101.43				104.61	107.81	111.03	114.25	117.48	120.73	123.97	133.96
-0.078	96.21	96.95	99.22	102.33		105.50				108.69	111.90	115.13	118.36	121.60	124.86	128.11	138.04
-0.080	100.38	101.12	103.39	106.51		109.68				112.89	116.11	119.34	122.58	125.83	129.08	132.36	142.31
-0.082	104.66	105.40	107.68	110.80		113.98				117.19	120.42	123.67	126.92	130.17	133.45	136.72	146.79
-0.084	109.05	109.90	112.08	115.21		118.40				121.62	124.86	128.11	131.37	134.63	137.90	141.19	151.30
-0.086	113.58	114.32	116.60	119.74		122.93				126.16	129.41	132.67	135.93	139.21	142.50	145.79	155.93
-0.088	118.22	118.96	121.24	124.39		127.58				130.82	134.09	137.35	140.62	143.91	147.19	150.50	160.70
-0.090	122.98	123.72	126.01	129.16		132.37				135.61	138.89	142.15	145.44	148.73	152.04	155.34	165.58
-0.092	127.87	128.61	130.91	134.06		137.28				140.52	143.81	147.08	150.38	153.68	156.98	160.30	170.59
-0.094	132.89	133.63	135.93	139.09		142.32				145.57	148.86	152.14	155.45	158.76	162.09	165.40	175.78
-0.096	138.05	138.79	141.09	144.26		147.49				150.75	154.05	157.34	160.65	163.97	167.29	170.64	180.94
-0.098	143.34	144.08	146.39	149.56		152.81				156.06	159.38	162.67	166.00	169.32	172.67	176.01	186.31
-0.100	148.78	149.52	151.82	155.00		158.74				161.52	164.85	168.15	171.48	174.82	178.15	181.52	191.82
-0.102	154.35	155.10	157.41	160.59		163.36				167.12	170.46	173.77	177.11	180.45	183.82	187.18	197.48
-0.104	160.05	160.80	163.11	166.29		168.10				172.00	175.34	178.67	182.00	185.34	188.67	192.00	202.30
-0.106	165.89	166.64	168.95	172.13		173.00				177.00	180.34	183.67	187.00	190.34	193.67	197.00	207.30
-0.108	171.84	172.59	174.90	178.08		178.00				181.00	184.34	187.67	191.00	194.34	197.67	201.00	211.30
-0.110	177.91	178.66	180.97	184.15		183.00				185.00	188.34	191.67	195.00	198.34	201.67	205.00	215.30
-0.112	184.10	184.85	187.16	190.34		188.00				189.00	192.34	195.67	199.00	202.34	205.67	209.00	219.30
-0.114	190.41	191.16	193.47	196.65		193.00				194.00	197.34	200.67	204.00	207.34	210.67	214.00	224.30
-0.116	196.84	197.59	199.90	203.08		198.00				199.00	202.34	20					

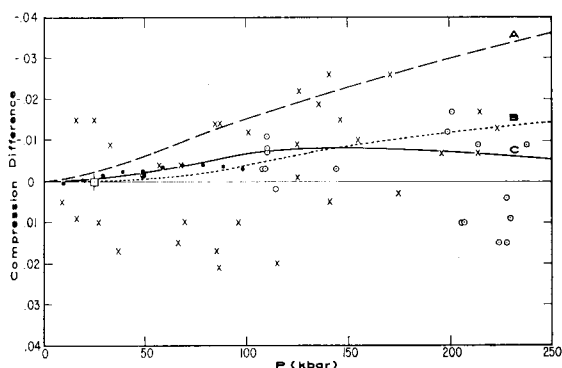


FIG. 1. Comparison of calculated and measured compressions as a function of pressure for NaCl. The ordinate is $\Delta V/V_0$ calculated by Decker minus $\Delta V/V_0$ calculated or measured by others. Curve A is Murnaghan's equation with B_0 and B_0' taken from Ref. 8. Curve B is Murnaghan's equation with B_0 as in A but $B_0' = 4.60$. Curve C is calculated by Perez-Albuerne and Drickamer, Ref. 3. ● smoothed data from Bridgman, Ref. 4. × measurements by Perez-Albuerne and Drickamer, Ref. 3. ○ dynamic measurements by Christian, Ref. 5. □ measurement by Jeffery *et al.*, Ref. 6.

pressure, making the Murnaghan equation a poor equation of state at higher pressures. The experimental data is, however, too scattered to make a choice between the equations of Perez-Albuerne and Drickamer, and the results calculated in Ref. 1 and tabulated in Table I.

I wish to thank Dr. J. Dean Barnett for his help in preparing the table and encouragement in this work.

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Lorentz Microscopy of Growing Domains in Permalloy Films

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QUANTITATIVE measurements of domain growth in evaporated, strain-sensitive Permalloy 66:34 Ni-Fe films of low coercivity have been made using Lorentz electron microscopy.^{1,2} Magnetic ripple¹ was absent under low axial and radial magnetic fields and present when a small axial field was applied. When magnetic ripple is absent, stages in domain growth can be shown by expressing domain area as a function of the applied field.

For the measurement of domain growth in strain-sensitive materials, it is desirable to have: High resolution by normal electron microscopy and diffraction, an accurate value for the transverse field applied to the specimen, and a low axial field. Previously, measurements have been made in RCA microscopes with an attachment using only a projector lens^{3,4} or in a special specimen holder with axial field coils.⁵ The attachment^{3,4} gives only low magnifications and the film cannot be observed readily by normal microscopy. The specimen holder, while it allows of normal optics, has mainly an axial rather than a transverse field and the transverse component is difficult to measure. A specimen holder was designed which combined the good features of both methods. The specimen holder is shown in Fig. 1. It is made from a standard RCA part; the specimen holder and cap have been machined to provide space for two miniature coils. Each coil consists of 17 layers of No. 38 Solderize wire with 12 turns per layer wound on

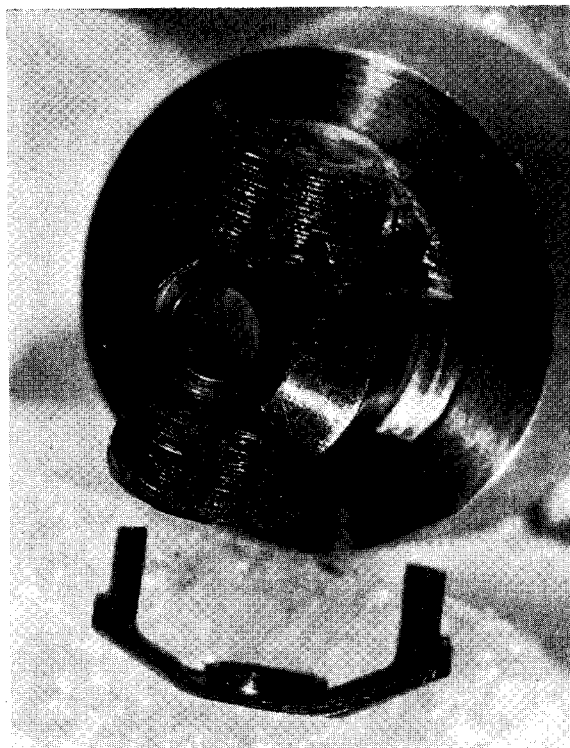


FIG. 1. A modified sample holder for Lorentz microscopy of thin ferromagnetic films in the RCA EMU-3 electron microscope.

a machined Teflon bobbin. The outer radius of each bobbin is 0.098 in. and its length 0.028 in. The specimen is held at the center of the coils by a small brass cylinder and secured with the cap. The power supply consists of a 12-V battery, a polarity reversing switch, and voltage divider.⁶ Solenoid current is measured with an ammeter (1.0 A, full scale).

The Helmholtz coils are calibrated using a Hall-effect probe at the specimen level. A maximum field of 120 Oe is obtained for a current of 800 mA. The magnetic field is linear with current and close to the calculated values for the Helmholtz coils.

In operation it is found that the image displacement produced by the miniature Helmholtz coils is easily corrected by a slight lateral movement of the specimen. The advantages of this holder are: Normal operation to $\times 30\,000$ magnification can be immediately obtained, and selected-area diffraction readily used. Low magnifications of $\times 500$ are obtained by reducing the current in the projector lens. The field applied to the specimen is known with accuracy, the optical system of the microscope is not changed appreciably, and it is possible to change rapidly to high magnifications and selected-area diffraction. Previous sample holders have had the film well above the normal specimen position, and use two or three Helmholtz coils to compensate for deviation of the electron beam.^{6,7} An axial coil has previously been used in the normal specimen position but has the disadvantage that measurement of absolute values cannot be easily made.⁸ Special Lorentz attachments have also been used but do not provide an immediate change to selected-area diffraction and normal high magnification microscopy^{3,4} since only a projector system is used.

Permalloy films were prepared by evaporation of premelted 66.19 Ni-33.81 Fe alloy onto a freshly cleaved rocksalt crystal held at 300°C, in a vacuum of 5×10^{-6} Torr. The deposition field was 50 Oe. Film thickness is 800 Å by Tolansky interferometric measurements. Films were floated off, mounted, and examined in the RCA-3G electron microscope at 100 kV.

Films were found to have a well-defined uniaxial anisotropy in the direction of the field applied during the evaporation. This ob-