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On the use of a modified square-well model for prediction and correlation of thermal diffusion factors in binary liquid mixtures

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Recently reported thermal diffusion factors obtained from heats of transport have been used to test the ability of existing theories to predict thermal diffusivities using model parameters regressed from pure component transport data. None of the theories tested were able to provide even qualitative agreement with experiment. However, predictions using a square-well Enskog theory, modified here for consistency with normal experimental definitions, were found to be approximately correct using pure-component square-well parameters regressed from viscosity and thermal conductivity and an assumed mixing rule for cross terms. Predicted values are very sensitive to the energy mixing rule, and correlation of experimental data is possible for some systems using this theory with one adjustable parameter in the mixing rule.

I. INTRODUCTION

In a companion paper to this one,¹ we reported measurement of heats of transport in binary mixtures containing carbon tetrachloride and benzene, toluene, 2-propanone, *n*-hexane, and *n*-octane at 298.15 and 308.15 K at ambient pressure. A previous study² reported heats of transport for mixtures of carbon tetrachloride with certain straight- and branched-chain C6 through C8 paraffins. Heats of transport represent the magnitude of the heat flux produced by molecular diffusion of the constituents in response to a chemical potential gradient. Using thermodynamic information concerning the composition dependence of the activity coefficient in these mixtures and Onsager reciprocity, we calculated thermal diffusion factors from the measured heats of transport. As cross-transport coefficients, thermal diffusion factors (or equivalently, heats of transport) have been considered by some^{3,4} to be extremely sensitive to the molecular interactions in solution. Thus, simulation of thermal-diffusion or heat-of-transport data may lead to refined models for intermolecular potential wells or better values and mixing rules for their parameters. The previous two studies provide sufficient data to provide preliminary tests of existing models.

II. THEORIES FOR THE THERMAL DIFFUSION FACTOR

Several theoretical approaches have been advanced for the heat of transport and/or thermal diffusion factor. Based on Kirkwood's Brownian motion method, Bearman *et al.*⁵ developed an expression for heats of transport for systems in which (1) particles react with central forces only, (2) intermolecular potentials can be written as sums of pair potentials, and (3) both components possess only translational energy. The heat of transport for such a system in the absence of external fields is

$$Q_T^* = Q_{T1}^* + Q_{T2}^*, \quad (1)$$

where Q_T^* is the heat of transport, Q_{T1}^* is a term involving averages over equilibrium ensembles, and Q_{T2}^* involves perturbations of the equilibrium distribution due to the flow of

heat and matter. The expressions for Q_{T1}^* and Q_{T2}^* are complex, but Bearman *et al.* were able to simplify them for the particular case of regular solutions. Under this simplification the expressions are

$$Q_{T1}^* = \frac{1}{2} \left(\frac{m_1 x_1}{m_2} + x_2 \right) \left(\frac{\bar{v}_1 \bar{v}_2}{\bar{v}} \right) \left(\frac{\bar{L}_2}{\bar{v}_2} - \frac{\bar{L}_1}{\bar{v}_1} \right), \quad (2)$$

$$Q_{T2}^* = \frac{1}{2v} \left(\frac{D_2 - D_1}{D_2 + D_1} \right) \left(\frac{m_1 x_1}{m_2} + x_2 \right) \left\{ \bar{v}_1 \bar{v}_2 \left(\frac{\bar{L}_2}{\bar{v}_2} + \frac{\bar{L}_1}{\bar{v}_1} \right) + 2x_1 (\bar{L}_1 x_1 - \bar{L}_2 x_2) + 2x_2 (\bar{L}_2 \bar{v}_2 - L_2 v_2) - \frac{2}{3} \int r \left(\frac{d\phi_{12}}{dr} - 1 \right) V'_{21} g'_{21} d^3 r \right\}, \quad (3)$$

where $\bar{v}$ is the mean molecular volume, $\bar{v}_i$ is the partial molecular volume of component i , v_i is the molecular volume of pure component i , $\bar{L}_i$ is the partial enthalpy departure function of component i relative to the ideal gas state, L_i is the enthalpy departure function of pure component i relative to the ideal gas state, m_i is the molecular mass of component i , D_i is the self-diffusion coefficient of component i in the mixture, and x_i is mole fraction of component i . The integral in Eq. (3) has never been evaluated for real systems because it contains the radial distribution function g'_{12} , the derivative of intermolecular potential with respect to position V'_{21} , and the nonequilibrium radial distribution function ϕ_{12} .

An elementary transition state theory (ETST) has also been developed by Mortimer and Eyring⁶ for calculation of thermal diffusion factors α . In terms of the standard state molar enthalpy $\Delta H^\ddagger$ and entropy $\Delta S^\ddagger$ changes for component i in the activation process as molecule 1 moves from the initial uniform state to the high-potential-energy transition state, Mortimer and Eyring write

$$\alpha_{(\text{ETST})} = \frac{\Delta H^\ddagger_1 e^{-\Delta H^\ddagger_1/RT} - \Delta H^\ddagger_2 e^{(\Delta S^\ddagger_2 - \Delta S^\ddagger_1)/R} e^{-\Delta H^\ddagger_2/RT}}{RT [x_2 e^{-\Delta H^\ddagger_1/RT} + x_1 e^{(\Delta S^\ddagger_1 - \Delta S^\ddagger_2)/R} e^{-\Delta H^\ddagger_2/RT}]}. \quad (4)$$

In this method, the thermal diffusion factor not only depends on temperature and concentration, but also on the activation parameters. Theoretically, the latter three quanti-

ties can be fitted by regression of three or more values of α as a function of composition and temperature. Unfortunately, the sum of the squares of the residuals appears to be a complicated function of the parameters, containing various saddle points and several relative extrema, and confidence in their physical meaning wanes when they are obtained in this manner.

Guy⁷ proposed the following expression for the thermal diffusion factor

$$\alpha^{(\text{Guy})} = \frac{M_2(h_2^E - h_1^E)}{RT(1 + \Gamma_{22})}, \quad (5)$$

where M_2 is the molecular weight of the less dense of the two components, h_i^E is the partial excess enthalpy of component i , and Γ_{ii} is the so-called thermodynamic factor which is related to the activity coefficient of component i (relative to pure-component standard state) γ_i by

$$\Gamma_{ii} = \left(\frac{\partial \ln \gamma_i}{\partial \ln x_i} \right)_{T,P}. \quad (6)$$

Guy reported reasonable results using Eq. (6) on a single binary system.

The first kinetic theory for a dense hard-sphere fluid was due to Enskog⁸ who generalized the Boltzmann equation to describe hard-sphere dynamics in the dense regime. This theory, commonly called the standard Enskog theory (or SET), was later extended to binary⁹ and multicomponent¹⁰ dense hard-sphere fluid mixtures. For a binary,

$$\alpha^{(\text{SET})} = \frac{5}{2g_{12}} \left[(n/n_2)m_1^{-1/2}K_1(a_{01}a_{-1-1} - a_{0-1}a_{1-1}) + (n/n_1)m_2^{-1/2}K_2(a_{0-1}a_{11} - a_{01}a_{1-1}) \right] / (a_{11}a_{-1-1} - a_{1-1}^2), \quad (7)$$

where the function K_i is defined by

$$K_i = 1 + \left(\frac{1}{2} \right) \sum_{j=1}^2 b_{ij}g_{ij}M_{ij}M_{ji}. \quad (8)$$

Here,

$$b_{ij} = 2\pi n_j \sigma_{ij}^3 / 3, \quad (9)$$

$$M_{ij} = \frac{m_i}{(m_i + m_j)}, \quad (10)$$

$$\sigma_{ij} = \frac{1}{2}(\sigma_i + \sigma_j), \quad (11)$$

$$\rho = m_1 n_1 + m_2 n_2, \quad (12)$$

m_i is molecular mass, n_i is number density, σ_i is the hard-sphere diameter of component i , and a_{rs} are Sonine polynomial coefficients calculatable from the equations given by Chapman and Cowling.¹¹

Unfortunately, SET does not agree with Onsager reciprocity.¹² Additionally, Kincaid *et al.*¹³ found that SET led to nonphysical values for the mutual diffusion coefficient. Several authors have resolved this inconsistency by redefining the diffusional driving forces to agree with those commonly used in irreversible thermodynamics definitions. Barajas *et al.*¹² obtained a revised Enskog theory (or RET1) for the thermal diffusion factor,

$$\alpha^{(\text{RET1})} = \left(\frac{M_1 M_2}{M^2(1 + \Gamma_{11})} \right) \left[\alpha^{(\text{SET})} + \frac{2\pi}{3} \left(n_1 \sigma_1^3 - n_2 \sigma_2^3 + 2 \frac{m_2 n_2 - m_1 n_1}{m_1 + m_2} \sigma_{12}^3 \right) \right]. \quad (13)$$

Similarly, Lopez de Haro *et al.*¹⁴ obtained a revised Enskog theory (or RET2) for the thermal diffusion factor in terms of the derivative of the chemical potential with respect to composition. In this theory, α is given by

$$\alpha^{(\text{RET2})} = \frac{m_1 n^3 \left\{ \sum_{k=1}^2 d_{1,0}^{(k)} / n \sum_{j=1}^2 n_k (\delta_{kj} + 2\rho b_{kj} M_{kj} g_{kj}) - E_{k2} / P_2 \sum_{p=1}^2 n_p (\delta_{pj} + 2\rho b_{pj} M_{pj} g_{pj}) - a_0^{(1)} \right\}}{\rho n_1 n_2 \sum_{k=1}^2 d_{1,0}^{(k)} (E_{k1} - P_1 / P_2 E_{k2})}, \quad (14)$$

where

$$E_{ij} = \frac{n_i}{kT} \left(\frac{\partial \mu_i}{\partial n_j} \right)_{T, n_k \neq j}, \quad (15)$$

$$P_i = \sum_{j=1}^2 E_{ji}, \quad (16)$$

and $d_{1,0}^{(k)}$ and $a_0^{(1)}$ are Sonine coefficients. In this theory, the Sonine coefficients are calculated to third order from the equations given by Lopez de Haro *et al.*¹⁴

As mentioned, the thermal diffusion factor is expected to be very sensitive to the form of the intermolecular potential and the values of the parameters therein. The hard-sphere theory represents the simplest evaluation of the Enskog theory, but solutions based on more realistic potentials are desirable. Davis *et al.*¹⁵ developed a transport equation for the singlet distribution function which is essentially a modified form of the equation derived by Enskog for dense hard spheres. McLaughlin and Davis¹⁶ extended the square-well theory to binary mixtures. Following the Chapman-Enskog procedure, McLaughlin and Davis derived for the square-well model (SWM)

$$\alpha^{(\text{SWM})} = \left(\frac{5n}{2} \right) \left[\frac{F_1(a_{01}a_{-1-1} - a_{0-1}a_{1-1})}{n_2 m_2^{1/2}} + \frac{F_2(a_{0-1}a_{11} - a_{01}a_{1-1})}{n_1 m_2^{1/2}} \right] / (a_{11}a_{-1-1} - a_{1-1}^2) + \frac{nb_{12}\rho \zeta_{12}(M_1 - M_2)}{n_2} \quad (17)$$

with the following definitions:

$$F_i = 1 + \frac{3}{2} b_{ii} \rho \zeta_{ii} + \frac{1}{2} M_1 M_2 b_{ij} \rho \times [\zeta_{12} + M_j (M_j - M_i) \chi_{12} / \psi_{12}], \quad (18)$$

$$\psi_{ij} = 1 - \exp(\epsilon_{ij}/kT) + (\epsilon_{ij}/2kT) \zeta_{ij}, \quad (19)$$

$$\zeta_{ij} = 1 + \frac{4e^{(\epsilon_{ij}/kT)}}{\pi^{1/2}} \int_{\epsilon_{ij}/kT}^{\infty} e^{-x^2} dx, \quad (20)$$

$$\chi_{ij} = \frac{\epsilon_{ij}}{\pi^{1/2} kT} \left[\frac{J_1}{2} - \frac{J_3}{3} - \frac{J_1 \epsilon_{ij}}{3kT} \right], \quad (21)$$

$$J_n = \int_0^{\infty} x^n \sqrt{x^2 + \epsilon_{ij}/kT} e^{-x^2} dx, \quad (22)$$

$$\zeta_{ij} = g_{ij}(\sigma_{ij}^{(1)}) + \left(\frac{\sigma_{ij}^{(2)}}{\sigma_{ij}^{(1)}} \right)^3 g_{ij}(\sigma_{ij}^{(2)}) \psi_{ij}, \quad (23)$$

where $g_{ij}(\sigma_{ij}^{(1)})$ is the value of the radial distribution function evaluated just inside the potential well, $g_{ij}(\sigma_{ij}^{(2)})$ is the value just outside the well, and ϵ_{12} is the well depth between unlike species. In Eq. (17), the a_{rs} are Sonine polynomial coefficients for the square-well model which are calculatable to first order from the equations given by McLaughlin and Davis.¹⁶

III. RESULTS USING EXISTING MODELS

The efficacy of the various models discussed above was tested by comparison of calculated values to those obtained from the experimental work previously reported.^{1,2} In all but Guy's model, potential parameters are required for an assumed intermolecular potential model. This presents two problems: (1) comparison to experiment inseparably tests both the theory and the intermolecular potential model, and (2) intermolecular potential parameters must be available. The first situation means that disagreement with experimental data does not distinguish between failure of the theory and inappropriate choice of the pair potential model. The second situation means that the theory can be used to either correlate data (by regressing potential parameters from the experimental data) or to predict properties (by regressing

potential parameters from some other property and using those values in prediction of the desired property). We test the equations in a predictive capacity; parameters in the models are evaluated from other properties.

Bearman's method cannot be evaluated in its entirety because of the nonequilibrium radial distribution function appearing in Eq. (3). While a complete test of this method cannot be made, the equilibrium contribution may yield at least qualitatively correct predictions. Thus calculations were made for Q_{12}^* from Eqs. (1) and (2) where the partial molal quantities were evaluated from compiled data.¹⁷ Table I shows the results obtained from this procedure in comparison to experimental values.¹ Bearman and Horne¹⁸ also assumed that Q_{12}^* is negligible in their calculations and found that calculated values were too low by 50% or more. Our results for the systems shown in Table I are in agreement with the findings of Bearman and Horne that the equilibrium portion is generally only a fraction of the experimental value, and it may even have the wrong sign.

The absolute reaction rate theory calculations require activation parameter data as shown in Eq. (4). To retain this as a predictive method, $\Delta H_1^\ddagger$, $\Delta H_2^\ddagger$, and $(\Delta S_2^\ddagger - \Delta S_1^\ddagger)$ were regressed from the model's viscosity equation.¹⁹ This assumes that the activation parameters are the same for viscous flow and diffusional processes. The results of the calculations are shown in Table I. In this case, the magnitudes are approximately right, but the signs are opposite those of the experimental data. It should be emphasized that disagreement of theory and experiment in this case only implies that predictions of α cannot be made from viscosity data. We do not imply that the model is wrong, only that the activation parameters cannot be obtained from other data and used to predict heats of transport.

The model proposed by Guy is of interest because of its simplicity. However, unlike all of the other models, it contains no nonequilibrium information. We believe that the heat of transport is physically inseparable from the diffusional mechanism in terms of the energy distributions of the components²⁰; a view which is inconsistent with this model. Calculations of α using Eq. (5) were made using h^E data obtained from Christensen *et al.*²¹ Activity coefficient data

TABLE I. Predictions of liquid thermal diffusion factors at 298.15 K and ambient pressure by various theories in comparison to experimental values

w_1	$\alpha^{(\text{exp})}$	$\alpha^{(\text{Bearman})}$	$\alpha^{(\text{ETST})}$	$\alpha^{(\text{Guy})}$	$\alpha^{(\text{SET})}$	$\alpha^{(\text{RET1})}$	$\alpha^{(\text{SWM})}$
Carbon tetrachloride (1) + benzene (2)							
0.1	2.41	-0.028	-1.98	0.100	0.44	-0.28	1.06
0.3	2.25	-0.028	-1.86	0.088	0.42	-0.26	1.14
0.5	1.70	-0.027	-1.72	0.062	0.39	-0.24	1.22
0.7	1.16	-0.027	-1.58	0.010	0.36	-0.20	1.30
0.9	0.74	-0.026	-1.41	-0.097	0.33	-0.15	1.38
Carbon tetrachloride (1) + <i>n</i> -hexane (2)							
0.1	2.55	0.054	...	0.261	0.35	-0.79	4.71
0.3	2.52	0.056	...	0.228	0.34	-0.71	5.04
0.5	2.15	0.059	...	0.193	0.34	-0.65	5.46
0.7	1.93	0.062	...	0.051	0.34	-0.56	5.96
0.9	1.59	0.068	...	-0.367	0.33	-0.53	6.25

for Eq. (6) were obtained from the Wilson equation with parameters obtained from vapor liquid equilibrium data.²² The results are again shown in Table I. Values obtained from this model are inconsistent with experimental data. Not only is the magnitude of the predictions in error, but the sign is also sometimes wrong.

Application of the various Enskog or kinetic models in a predictive mode requires that intermolecular pair-potential parameters be regressed from other data. For hard-sphere calculations, we regress the pure-component hard-sphere diameters from pure-component thermal conductivity data in accordance with the Enskog model for thermal conductivity.²³ Values obtained were 5.43, 5.27, and 6.06 Å for carbon tetrachloride, benzene, and *n*-hexane, respectively. The mixing rule for hard spheres, Eq. (11), is used for σ_{ij} . Using Eq. (7) for SET and Eq. (13) for RET1, we again compare calculated and experimental values in Table I. All α values were about an order of magnitude too small for both models, while RET1 values were also of the wrong sign. The low SET results are consistent with the low SET predictions found by Palyvos *et al.*²⁴ for the argon + krypton system. Values for RET2 are not shown in Table I due to the difficulties in accurately evaluating the E_{ij} and P_i defined in Eqs. (15) and (16). Calculations were made using experimental data and the Wilson equation to obtain the chemical potentials, but the results were very poor.

From Table I, it would seem that SWM [Eqs. (17)–(23)] is more promising than the hard-sphere models due to its more realistic potential. However, SWM was arrived at in the usual SET manner. Thus, it employs diffusional driving forces which are inconsistent with those used in the irreversible thermodynamics definitions of transport coefficients. Values calculated from these equations would not, therefore, be consistent with experimental values. To make predictions using the square-well model, we first fitted pure component ϵ and σ values by simultaneous regression of pure-component thermal conductivity and viscosity data using the square-well model for those properties given by Reed and Gubbins.²⁵ Cross-interaction terms were calculated using an average mixing rule for σ and a geometric mixing rule for ϵ with the ratio of the well distances fixed at 1.8 as shown below:

$$\sigma_{ij}^{(k)} = (\sigma_{ii}^{(k)} + \sigma_{jj}^{(k)})/2, \quad (24)$$

$$\epsilon_{ij} = k(\epsilon_{ii}\epsilon_{jj})^{1/2}, \quad (25)$$

$$\sigma_{ij}^{(2)}/\sigma_{ij}^{(1)} = 1.8. \quad (26)$$

Values of pure-component square-well potential parameters obtained in this study are shown in Table II.

It is evident from Table I that with the possible exception of SWM no existing model can be used satisfactorily for prediction of α .

IV. MODIFICATION OF THE SQUARE-WELL MODEL

We have modified the square-well model in the same manner that Barajas *et al.*¹² modified SET for hard spheres. Using their definition of the diffusional driving force we obtain

TABLE II. Square-well potential parameters regressed from pure component thermal conductivity and viscosity data at 298.15 K and ambient pressure.

Component	$\sigma^{(1)}$ (Å) ^a	ϵ/k (K)
Carbon tetrachloride	2.21	122.7
Chloroform	4.62	307.5
Acetone	2.03	127.5
Benzene	2.14	123.7
Toluene	2.28	121.0
<i>n</i> -hexane	5.85	228.1
<i>n</i> -heptane	6.15	252.7
<i>n</i> -octane	6.20	304.7
3-methylpentane	5.81	226.5
2,3-dimethylpentane	6.02	250.1
2,2,4-trimethylpentane	6.16	288.6

^a $\sigma^{(2)} = 1.8\sigma^{(1)}$.

$$\alpha^{(\text{MSWM})} = \left(\frac{M_1 M_2}{M^2 (1 + \Gamma_{11})} \right) \left[\alpha^{(\text{SWM})} + \frac{2\pi}{3} \left(n_1 \sigma_{11}^{(1)^3} - n_2 \sigma_{22}^{(1)^3} + 2 \frac{m_2 n_2 - m_1 n_1}{m_1 + m_2} \sigma_{12}^{(1)^3} \right) \right] \quad (27)$$

for the modified-square-well model (MSWM), where $\alpha^{(\text{SWM})}$ represents Eqs. (17)–(23). This expression is exactly analogous to Eq. (13).

While Lebowitz²⁶ has solved the Percus–Yevick equation for a mixture of hard spheres, there is no exact expression for the radial distribution function of square-well fluids. For contact encounters in a hard-sphere binary mixture, the radial distribution functions are

$$g_{ii}^{\text{hs}}(\sigma_{ii}^{(1)}) = \frac{[1 + 0.5\xi + 1.5\eta_j \sigma_{jj}^{(1)^2} (\sigma_{ii}^{(1)} - \sigma_{jj}^{(1)})]}{(1 - \xi)^2}, \quad (28)$$

$$g_{ij}^{\text{hs}}(\sigma_{ij}^{(1)}) = [\sigma_{ii}^{(1)} g_{ii}(\sigma_{ii}^{(1)}) + \sigma_{jj}^{(1)} g_{jj}(\sigma_{jj}^{(1)})]/2\sigma_{ij}^{(1)}, \quad (29)$$

in which

$$\xi = \sum_{i=1}^2 \eta_i \sigma_{ii}^{(1)}, \quad (30)$$

and

$$\eta_i = \pi n_i / 6. \quad (31)$$

In the square-well theory,²⁷ these hard-sphere functions are augmented by an exponential factor

$$g_{ij}^{\text{sw}}(\sigma_{ij}^{(1)}) = g_{ij}^{\text{hs}}(\sigma_{ij}^{(1)}) \exp(\epsilon_{ij}/kT). \quad (32)$$

The functions $g_{ij}(\sigma_{ij}^{(2)})$ are complicated to compute. Throop and Bearman²⁸ have performed numerical calculations for these functions and found that for liquid densities

$$0.8 < g_{ij}^{\text{hs}}(\sigma_{ij}^{(2)}) < 1.1. \quad (33)$$

As a result of this apparently limited range over which $g_{ij}^{\text{hs}}(\sigma_{ij}^{(2)})$ may vary, the approximation

$$g_{ij}^{\text{hs}}(\sigma_{ij}^{(2)}) = 1.0 \quad (34)$$

should introduce only small errors into the computed transport coefficients. Sample calculations indicate that this error does not exceed about 3%. Consequently, the approximation represented by Eq. (34) is used in all of our square-well computations.

FIG. 1. Experimental (●) and predicted (—, $k = 1$; ---, $k = 1.68$) values of the thermal diffusion factor for the carbon tetrachloride (1) + acetone (2) system at 298.15 K and ambient pressure.

FIG. 4. Experimental (●) and predicted (—, $k = 1$; ---, $k = 0.92$) values of the thermal diffusion factor for the carbon tetrachloride (1) + *n*-hexane (2) system at 298.15 K and ambient pressure.

FIG. 2. Experimental (●) and predicted (—, $k = 1$; ---, $k = 1.15$) values of the thermal diffusion factor for the carbon tetrachloride (1) + benzene (2) system at 298.15 K and ambient pressure.

FIG. 5. Experimental (●) and predicted (—, $k = 1$; ---, $k = 0.95$) values of the thermal diffusion factor for the carbon tetrachloride (1) + *n*-heptane (2) system at 298.15 K and ambient pressure.

FIG. 3. Experimental (●) and predicted (—, $k = 1$; ---, $k = 1.14$) values of the thermal diffusion factor for the carbon tetrachloride (1) + toluene (2) system at 298.15 K and ambient pressure.

FIG. 6. Experimental (●) and predicted (—, $k = 1$; ---, $k = 1.30$) values of the thermal diffusion factor for the carbon tetrachloride (1) + *n*-octane (2) system at 298.15 K and ambient pressure.

FIG. 7. Experimental (●) and predicted (—, $k = 1$; ---, $k = 0.80$) values of the thermal diffusion factor for the carbon tetrachloride (1) + 3-methylpentane (2) system at 298.15 K and ambient pressure.

FIG. 8. Experimental (●) and predicted (—, $k = 1$; ---, $k = 1.18$) values of the thermal diffusion factor for the carbon tetrachloride (1) + 2,2,4-trimethylpentane (2) system at 298.15 K and ambient pressure.

V. DISCUSSION OF RESULTS

In all of the calculations for this MSWM we used the *ad hoc* mixing rules of Eqs. (24)–(26). With $k = 1$ the method is predictive since all of the constants are obtained from pure component thermal conductivity and viscosity data. The method can also be used in a correlative mode by regressing a value for k in the mixing rule from experimental α values. We have performed both types of calculations and the results are shown in Figs. 1–8.

As a predictive model, MSWM may still be in error by a factor of 2 or more, but it is considerably better than any of the other methods available. It predicts the gross composition dependence of α quite well, and can be used to obtain approximate values. The finer detail of the composition dependence of this model is inherent in the *ad hoc* mixing rule for ϵ ; it is perhaps not surprising that better accuracy is not obtained. As shown in Figs. 1, 2, 6, and 8, considerable flexibility is provided by adjusting the mixing rule for ϵ , and reasonable agreement can be obtained in some cases when k is regressed from the experimental data. The values of α are

indeed quite sensitive to the cross term of the energy parameter, and measurement of thermal diffusion factors or heats of transport can provide useful information in refinement of a potential model. The ability of this model to correlate and predict α using parameters obtained from pure transport properties suggests the importance of more extensive studies on other systems in an attempt to develop a general mixing rule.

VI. CONCLUSIONS

We have used recently measured heat-of-transport data in the form of thermal diffusion factors to test existing models and theories. None of the existing methods were capable of even qualitatively predicting thermal diffusion factors using parameters regressed from pure component transport properties. This is not necessarily an indictment of those theories since there is no way to distinguish between failure of the model and of the assumed potential. However, we have modified the square-well model of Davis in accordance with the technique used by Barajas so that α agrees with the usual experimental definition. Using this method and square-well potential parameters regressed from pure component transport properties, we were able to obtain approximate agreement with experiment. It was found that calculated α values are very sensitive to the mixing rule used for ϵ . This implies that heat-of-transport or thermal-diffusion experiments can be used as a sensitive probe of intermolecular potentials. In particular, it was found that slight adjustment of a constant in the mixing rule for ϵ enabled improved correlation of measured α values for about half the systems studied.

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